Coupled effects of ocean current on wind stress in the Bay of Bengal: Eddy energetics and upper ocean stratification

Hyodae Seo\textsuperscript{a,}\textsuperscript{*}, Aneesh C. Subramanian\textsuperscript{b}, Hajoon Song\textsuperscript{c}, Jasti S. Chowdary\textsuperscript{d}

\textsuperscript{a} Woods Hole Oceanographic Institution, Woods Hole, MA, USA
\textsuperscript{b} University of Colorado, Boulder, CO, USA
\textsuperscript{c} Yonsei University, Seoul, Republic of Korea
\textsuperscript{d} Indian Institute of Tropical Meteorology, Pune, India

A B S T R A C T

This study examines the effect of surface current in the bulk formula for the wind stress, referred to as the relative wind (RW) effect, on the energetics of the geostrophic circulation and the upper ocean stratification in the Bay of Bengal (BoB) during the summer monsoon seasons. When the RW effect is taken into account in the high-resolution SCOAR (WRF-ROMS) regional coupled model simulation and compared to the run without such a consideration, the kinetic energy both in the mean (MKE) and eddy (EKE) is reduced by more than a factor of two. The most significant reduction in the kinetic energy is found along the path of the northward East India Coastal Current (EICC) and to the south of its separated latitude. The energetics calculations and spectral analysis reveal that this significant damping of EKE is primarily due to reduced eddy wind work principally at wavelengths close to the first baroclinic Rossby deformation radius, indicating the modulation of the wind work by geostrophic mesoscale eddy fields. Moreover, the mixed layer depth (MLD) is significantly shoaled south of the separated EICC latitude, the area dominated by anticyclonic eddy activity. The shallower mixed layer and enhanced stratification with the RW effect are attributed to the anomalous upward Ekman velocity, which itself is generated by the interaction of anticyclonic mesoscale surface current and the prevailing southwest monsoonal wind. Overall, the geostrophic circulation and upper ocean stratification along the EICC and south of its separated latitude exhibit the most significant dynamical response. This result implies that this southwestern part of the BoB is a hot spot for the momentum exchange between the surface circulation and the monsoonal winds, thus a potential area for focused field measurements for the ocean circulation energetics and air-sea interaction.

1. Introduction

The mechanical work done by the wind stress on the ocean surface current represents the most significant source of kinetic energy input to the quasi-steady circulation of the oceans (Wunsch, 1998). According to the bulk aerodynamic formula, the wind stress ($\tau$) is calculated as

$$\tau = \rho_a C_D (u_a - u_o) |u_a - u_o|$$

where $\rho_a$ the density of the air, $C_D$ the drag coefficient, $u_a$ and $u_o$ the wind and ocean surface current velocity, respectively. The term $u_a - u_o$ indicates that the wind stress is determined by the velocity shear across the air-sea interface, not just by the wind. Hereinafter, this will be referred to as the relative wind (RW) effect.

The previous studies have shown that considering the RW effect in the stress formulation produces the wind work that is consistently smaller than the case without consideration of the RW effect. For example, the scaling analysis by Duhaut and Straub (2006) suggests the wind work be reduced by 20% due to the RW effect. More importantly, they showed that the length-scale at which this 20% reduction in the wind work takes place co-occurs with the same length-scale that contains the bulk of oceanic kinetic energy, which implies a linear, scale-to-scale damping effect of the kinetic energy. This damping effect has been espoused by several modeling studies of varying complexity ranging from a quasi-geostrophic ocean model (Hutchinson et al., 2010), ocean general circulation models (Pacanowski, 1987; Zhai and Greatbatch, 2007; Eden and Dietze, 2009; Anderson et al., 2011), coupled general circulation models (Luo et al., 2005) and to more recent high-resolution regional coupled models (Seo et al., 2007b, 2016; Small et al., 2009; Renault et al., 2016a,b; Seo, 2017). In particular, the results from high-resolution regional coupled models have ascertained that the damping of the ocean kinetic energy by the RW effect, which amounts to 20–50% of the climatology, is particularly efficient over the swift boundary currents, their extensions, and the associated energetic mesoscale eddy fields.

Since the ocean current affects the wind stress, the surface current and the vorticity fields can create changes in Ekman vertical velocities (Thomas and Rhines, 2002; McGillicuddy, 2015). These anomalous Ekman vertical velocities also act to damp the eddy activity by producing Ekman upwelling within the anticyclones (Dewar and Flierl, 1987; Martin and Richards, 2001) and downwelling in the interior of...
cyclones (Gaube et al., 2015; Seo et al., 2016). Thus, the RW effect is manifested not just in the wind work but also in the Ekman pumping, affecting the oceanic internal instability by displacing the thermocline and the eddy kinetic energy fields.

Recent studies based on satellite observations have also allowed the opportunity to separate this wind-current, or mechanical, coupling effect from the SST-wind thermal coupling effect, the latter of which is shown to be particularly strong at oceanic mesoscales and frontal scales (Chelton, 2013; Gaube et al., 2015). Using the high-resolution model simulations, Seo et al. (2016) demonstrated that the dynamical response in the ocean mesoscale fields to these two types of coupling, mechanical and thermal, is highly distinctive. The mechanical coupling consistently works to reduce the energetics of the currents, whereas the thermal coupling, especially at oceanic mesoscale scales, tends to shift the eddy fields (see also Seo, 2017). A recent study based on mesoscale resolving coupled model simulations (Renault et al., 2018) further suggested that these two types of coupling are highly scale-dependent, demonstrating that the mechanical coupling is far more effective at the length-scale approaching the oceanic submesoscales.

This study, based on the Bay of Bengal (BoB) during the summer monsoon seasons, attempts to quantify the effect of air-sea coupling on the energetics of the monsoon circulation. We will consider only the mechanical coupling effect in this study, while the thermal coupling is deferred as a future study. However, the BoB, unlike other oceanic boundary currents and their extensions addressed in the previous studies, features a relatively weak expression of the eddy and boundary currents in the SST fields, so we might expect the resulting thermal coupling to be relatively small. Furthermore, it is currently unknown in the literature what the appropriate satellite-based coupling coefficient might be that relates the crosswind SST gradient and wind stress curl, making it difficult to estimate and validate the SST gradient-induced Ekman pumping velocity from the model simulations. However, knowing the recent evidence that points to the importance of the small-scale SST fronts (e.g. Samanta et al., 2018), all these issues related to thermal coupling remain to be further investigated.

The BoB is an ocean basin surrounded by the landmass to the west, north, and east, so all the water mass exchange with the northern Indian Ocean takes place through the southern open boundary via the seasonally reversing monsoon currents (Schott and McCreary, 2001; Shankar et al., 2002). The summertime (June–September, JJAS) surface circulation in the BoB is characterized by the intense and narrow East India Coastal Current (EICC), which, in summer, flows northward along the southern part of the east coast of India and the southward along the northern part (Shankar et al., 1996; Shankar, 2000; Shetye et al., 1990, 1993; Durand et al., 2009). The northward EICC in the southern part separates from the coast at around 16°N (Potemra et al., 1991; Sil and Chakraborty, 2011; Webber et al., 2018).

The interannual variability and the forcing mechanism of the EICC were investigated by Dandapat et al. (2018) using a numerical model, showing the importance of seasonal coastal Kelvin waves in the development of the EICC. Cheng et al. (2018) examined the eddy statistics and eddy generation mechanisms using satellite observations and a 1-1/2 layer reduced-gravity model to conclude that eddies are mainly generated in the eastern Bay (the tip of the Irrawaddy Delta off Myanmar) by equatorial intraseasonal wind, with nonlinear interaction with coastline geometry and bathymetry. The eddies subsequently propagate southwestward with a period of 30–120 days, and in the western boundary, especially along the EICC path, where the eddy kinetic energy (EKE) reaches the maximum due to enhanced baroclinic and barotropic instabilities that feed the eddy fields (Chen et al., 2018).

A distinguishing feature of the upper ocean structure of the BoB is its strong stratification, with the observed mixed layer depth (MLD) being of some of the shallowest in the world oceans (De Boyer Montégut et al., 2007), on the order of 30 m or less, due to the large freshwater flux inputs through local precipitation and river discharges (Seo et al., 2009; Durand et al., 2011; Chowdary et al., 2016). The previous ocean-modeling studies using different wind datasets or artificially increased or decreased strength of the wind forcing, have shown that the skillful simulations of the upper ocean circulation, eddy variability, and the upper ocean stratification in the ocean general circulation models depends highly on the detailed pattern and strength of the chosen wind forcing (e.g. Dey et al., 2017; Jana et al., 2018). Yet, none of these studies considered the RW effect, which as we will discuss, strongly modulates the wind stress and its curl.

The key results of our study are that the eddy activity is significantly reduced and the MLD significantly shoaled with the consideration of the RW effect. The fact that EKE is reduced may not be surprising. However, the magnitude of the reduction is remarkably large, yielding a factor of two difference in EKE. The shoaling of the MLD is primarily seen over the anticyclonic eddying region in the southwestern basin, where the RW effect generates the upward Ekman velocity, which domes the isopycnals above the thermocline and enhances the near-surface stratification.

2. Model and experiments

2.1. Regional coupled model

This study uses the Scripps Coupled Ocean-Atmosphere Regional (SCOAR) model (Seo et al., 2007a, 2014), which couples the Weather Research and Forecast (WRF; Skamarock et al., 2008) as its atmospheric component with the Regional Ocean Modeling System (ROMS; Haidvogel et al., 2000; Shchepetkin and McWilliams, 2005) as the ocean. The interacting boundary layer is based on the COARE bulk flux algorithm (Fairall et al., 1996, 2003), built in ROMS. The bulk meteorological variables and downward shortwave/longwave radiative fluxes from WRF and the SST and surface current from ROMS are used in the bulk formula to calculate the surface fluxes of heat, momentum, and freshwater every 3 h. The SCOAR model has been used in a wide range of air-sea studies in the Indian (Seo et al., 2008b, 2009, 2014; Seo, 2017), the Pacific (Seo et al., 2007a; Putrasahan et al., 2013a,b; Seo et al., 2016) and the Atlantic Oceans (Seo et al., 2006, 2007b; 2008a, 2017; Seo and Xie, 2011,2013).

The model domain covers the BoB north of 10°N (Fig. 1). The horizontal resolutions in WRF and ROMS are identical (5 km) with the matching grids and land-sea mask. The use of identical grids helps to better represent the eddy-forced air-sea flux variability in comparison to a more typical approach of coupling a coarse atmospheric model to a finer-scale ocean model. The use of identical grids has added benefits of eliminating interpolation errors in the surface fluxes near the coastal boundaries (e.g. Capet et al., 2004; Small et al., 2015) and, without the need for interpolation, improving the numerical efficiency of the coupler (Seo et al., 2009, 2016).

The 5-km resolution in the ocean is designed to better resolve the ocean mesoscale processes and the complex coastlines and estuaries. With the 5 km resolution in the atmosphere, the cumulus convective systems associated with the monsoons can be resolved explicitly. ROMS (WRF) is run with a stretched vertical grid with a total of 50 (35) vertical levels with approximately 15 (10) layers are allotted in the upper 150 m depth (below 750 m height).

Though the WRF model is run without parameterized convection, other processes are still parameterized. The cloud microphysics is represented by the WRF Single-Moment 3-class scheme (Hong et al., 2004) and the planetary boundary layer by the Yonsei University nonlocal scheme (Hong and Lim, 2006). The Rapid Radiation Transfer Model (RRTM; Mlawer et al., 1997) is used for longwave radiation transfer and the Dudhia broadband SW model (Dudhia, 1989) for the shortwave radiation scheme. The land surface process is treated with the Noah land surface model (Chen and Dudhia, 2001). In ROMS, the Mellor-Yamada level 2.5 turbulence closure scheme (Mellor and Yamada, 1982) with the equilibrium stability function of Kantha and Clayson (1994) determines vertical eddy viscosity and diffusivity. The
model does not include mixing parameterizations for the oceanic submesoscales and Langmuir turbulence. No explicit lateral mixing or diffusivity is applied, although the 3rd order upstream biased advection scheme introduces implicit numerical diffusivity (Haidvogel et al., 2000).

At the southern open boundary, the radiation and nudging method is applied to baroclinic components of velocity and tracers (Marchesiello et al., 2003; Di Lorenzo, 2003) with the stronger nudging on inflow (time scale of 10 days) than on outflow (120 days). The barotropic components of velocity are treated by Flather (1976) and the free surface by Chapman (1985). Though the eddy dynamics discussed in this study takes places close to the southern boundary, the simulated eddy and circulation features are consistent with several observational estimates and the previous numerical model simulations (Sec. 3a; Jana et al., 2018; Chen et al., 2018; Karmakar et al., 2018). Since the same boundary condition and open boundary treatment are applied to the control and sensitivity experiments and since this study concerns mainly the difference between the two runs, we contemplate that the proximity to the boundary will not change the interpretation of the results.

In ROMS, the freshwater inputs from the rivers are treated as point sources. The river discharges for the Ganges-Brahmaputra-Meghna (GBM) and the Irrawaddy are obtained from the updated monthly altimeter-based estimates of Papa et al. (2012). The discharge estimates of other rivers, such as the Krishna, Godavari, Mahanadi, Brahmani, Subarnareka, Hooghly, Sittang, and Salween, are based on monthly climatologies from Jana et al. (2015). The locations of point sources are manually selected based on the proximity of the resolved coastlines to the actual tributaries (Fig. 1; see also Jana et al., 2015; 2018). The total outflow rate is equally divided into the number of the point sources designated for each of the rivers except for the GBM. For the GBM, 80% of the total outflow is assigned to 15 river mouths east of 90°E, while the rest (20%) to 4 smaller rivers. The discharge is vertically distributed such that 95% of the total transport lies in the top 10 m. After preliminary sensitivity tests, the salinity of the river waters is set uniformly to 3 psu while the temperature is set to the climatological 2-m air temperatures (Jana et al., 2015). The sensitivity of the BoB circulation to the chosen river salinity values was explored by Jana et al. (2015, 2018), which demonstrated significant improvements in the representation of lifecycle of the freshwater plumes, advection of freshwater, and thus the near-surface stratification with the inclusion of river discharges.

### 2.2. Experimental setup

Before the WRF-ROMS coupled integrations, the 10-year ROMS spin-up simulation was conducted, with the lateral boundary condition from the climatology of the 5-daily Simple Ocean Data Assimilation (SODA; Carton and Giese, 2008) v3.4.1, which was forced by the ERA-Interim reanalysis (Dee et al., 2011) as the atmospheric forcing. The ROMS spin-up was also forced by the climatological monthly surface fluxes of momentum, heat, and freshwater based on the Comprehensive Ocean-Atmosphere Data Set (da Silva et al., 1994). After the 10-year spin-up, a 10-year hindcast simulation was conducted for 2006–2015 using the monthly ERA-Interim as the atmospheric forcing and the 5-daily SODA v3.4.1 data as the lateral boundary condition.

The ocean state on June 1 from the hindcast simulation was taken as the ROMS initial condition for the SCOAR WRF-ROMS coupled runs. In the coupled run, the 5-daily SODA v3.4.1 data continued to be the boundary condition for ROMS, while the WRF is initialized on June 1st 00Z and forced at the lateral boundary by the ERA-Interim. The two sets of SCOAR coupled runs were conducted for the summer months (June–September) for 9 years (2007–2015). These two sets of coupled runs differ only in how the wind stress is calculated in the bulk formula in Eq. (1). In CTL, the RW effect is considered in the wind stress calculation, whereas the importance of the RW effect can be diagnosed in

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![Model domain with the ocean bottom bathymetry (m) shaded in color. Also shown are the locations and number of the point sources of the river discharges, color-coded to represent each of the rivers. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)](image)
an otherwise identical calculation but with the RW omitted (noRW). The difference between CTL and noRW, or the effect of RW, is presented as the percent difference, defined as \((\text{CTL} - \text{noRW}) / \text{CTL} \times 100\). The significance of the difference is estimated using a Monte Carlo simulation, randomly scrambled 1000 times, to bootstrap error estimates for the statistical significance at 95%.

The effect of RW on the simulated flow fields can be immediately seen from Fig. 2, which compares the snapshot of the Rossby number \((\text{Ro})\), the relative vorticity, \(\zeta\), normalized by the local Coriolis frequency, \(f\) on June 12, 2009. Since this period is only 12 days after the initialization, the large-scale patterns of \(\text{Ro}\) remain similar, but one can notice that the absolute magnitude of \(\text{Ro}\) in CTL is generally weaker than that of noRW. The probability density function (PDF) of \(\text{Ro}\), calculated for the entire simulation period (9 summers) and over the whole domain, supports this initial impression.

\(\text{Ro}\) in excess of +0.5 is found in both runs; however, CTL shows more regions of smaller \(\text{Ro}\) and fewer areas of intense \(\text{Ro}\). The superposed black curve denotes the percent difference, confirming that \(\text{Ro}\) is reduced in CTL with the particularly strong reduction in the \(\text{Ro}\) range of \(-0.8\) to \(-0.5\). Therefore, the RW effect in the BoB appears to acts preferentially on the anticyclonic eddies with relatively high \(\text{Ro}\). The following sections will test this tentative conclusion and investigate in further detail the damping effect of the anticyclonic eddies and its scale dependence.

### 3. Results

#### 3.1. Changes in mean state

Fig. 3 compares the observed and simulated climatologies of the vectors and magnitude of wind stress and surface geostrophic current. The observed wind stress shows the prevailing southwesterly over the Bay with a maximum of 0.1 Nm\(^{-2}\) in the interior basin. The observed geostrophic current estimated from the SODA features the narrow northeasterward-flowing EICC in excess of 0.25 ms\(^{-1}\). The northward EICC separates from the coast at 16°N and continues northeasterward, while part of the flow recirculates southward anticyclonically, creating large horizontal velocity shear and enhanced eddy activity (Chen et al., 2018). This EICC featured in SODA is qualitatively consistent with other observational estimates such as the OSCAR and AVISO (Jana et al., 2018; Chen et al., 2018). Both CTL and noRW runs overestimate the strength of the observed wind stress. This can be attributed partly to a notable difference in resolution between the ERA-Interim (70 km) and the model (5 km). However, we also note that the ERA-Interim surface wind is already stronger compared to the scatterometer-based estimates of surface wind speed (not shown), implying that the overestimation would also be partly attributed to the pre-existing bias in the ERA-Interim, which is used as the lateral boundary condition. The geostrophic current from the models is more energetic than that inferred from SODA.

There are several notable differences in the climatologies between CTL and noRW, which we interpreted as the cumulative RW effect. The wind stress is reduced in CTL along the EICC but enhanced east and south of it. This difference in wind stress can be easily expected since over the EICC the geostrophic current is in the direction of the prevailing wind, which reduces the wind stress, while the converse is true for south of the EICC where the flow turns anticyclonically. This is the only region within the BoB where the wind stress is increased due to the RW effect, thus experiencing the higher turbulent kinetic energy (Section 3d). The modulation of wind stress by the surface current accounts for 10% of the mean value. In contrast, the difference in wind speed between CTL and noRW is negligible (<2%, not shown), suggesting that this reduction in wind stress is due to the consideration of the ocean current, not due to change in wind. Outside the region of strong current and eddies, the wind stress is only weakly reduced, and this change is insignificant at the 95% confidence level. The reduced wind stress over the EICC suggests that its circulation in CTL should be less energetic. Indeed, the EICC is substantially weaker in CTL with its maximum speed of 0.3 ms\(^{-1}\) in comparison to >0.6 ms\(^{-1}\) in noRW. There is also a significant difference in the magnitude of geostrophic current south of the separated EICC latitude.

#### 3.2. Changes in wind work

When the surface stress is modified by the ocean currents, the most direct response should be found in the wind work. The time-mean geostrophic wind work \((P_w)\) is defined following Stern (1975) as...
\[ P_g = \frac{1}{\rho_0} \langle \tau \cdot u_g \rangle, \]  
\[ (2) \]

where \( \rho_0 \) is the density of the sea water, \( u_g \) is the surface geostrophic current vectors, and the angled bracket denotes the time averaging (JJAS averages in each year). \( u_g \) can be broken down into the time mean and eddy components, where the eddy component, denoted as primes, is defined as the deviation from the time mean. Here, we ignore the modulation of wind work done on the surface waves (Wang and Huang, 2004) and as well as the Ekman current, which is not expected to produce significant motion within the general circulation (Wunsch, 1998; Von Storch et al., 2007; Scott and Xu, 2009). Then \( P_g \) becomes

\[ P_g = \left( \frac{\langle \tau \cdot u_g \rangle}{\rho_0} + \langle \tau' \cdot u_g' \rangle \right), \]

where \( P_{gm} (P_{ge}) \) represent the mean (eddy) geostrophic wind work, which will simply refer to as mean (eddy) wind work.

Fig. 4 compares the climatology of \( P_{gm} \) and \( P_{ge} \) between CTL and noRW, along with their zonally integrated meridional profiles. \( P_{gm} \) has the maximum positive value along the EICC path, where the geostrophic current is in the direction of the prevailing wind stress. Conversely, \( P_{gm} \) is negative to the south since the mean geostrophic current is in the opposite direction of the wind stress. When zonally integrated, \( P_{gm} \) is positive north of 12°N with the maximum at 15–16°N and negative south of 12°N. The magnitude of the reduction in the spatially integrated \( P_{gm} \) accounts for roughly 39% of the climatology in CTL (Table 1) and is most pronounced in the EICC region (Fig. 4c).

\[ P_{ge} \] is smaller than \( P_{gm} \) by a factor of 5, but it is an important term as it enters the EKE budget directly as either a source or sink. Between CTL and noRW, their absolute magnitudes remain comparable, but the sign switch from positive in noRW to negative in CTL. The negative \( P_{ge} \) in CTL means that the geostrophic eddies act as surface drag to the wind stress, thereby serving a sink of the eddy energy. This is in contrast to noRW, where this term is positive, acting as an additional energy source term. As is shown in the next section, this is the area of the EKE maximum and the largest changes in the EKE, implying an active role of mesoscale eddies in the modulation of wind work.

### Table 1

<table>
<thead>
<tr>
<th>Term</th>
<th>CTL</th>
<th>noRW</th>
<th>% difference</th>
</tr>
</thead>
<tbody>
<tr>
<td>( P_{gm} )</td>
<td>25.1</td>
<td>34.9</td>
<td>-39%</td>
</tr>
<tr>
<td>( P_{ge} )</td>
<td>13.9</td>
<td>12.3</td>
<td>-249%</td>
</tr>
<tr>
<td>BT</td>
<td>4.51</td>
<td>7.48</td>
<td>-63%</td>
</tr>
<tr>
<td>BC</td>
<td>7.36</td>
<td>7.36</td>
<td>12%</td>
</tr>
</tbody>
</table>

Fig. 3. The JJAS climatologies of (top) wind stress vectors and magnitude (Nm\(^{-2}\)) and (bottom) geostrophic surface current (ms\(^{-1}\)) from (left to right) observations, CTL and noRW. Dots denote the areas of significant difference at 95% confidence level, evaluated with the confidence interval obtained by a Monte Carlo bootstrap sampling (1000 times).

Fig. 4. Mean geostrophic wind work \( (P_{gm} = 10^6 \text{m}^3\text{s}^{-3}) \) from (a) CTL and (b) noRW, and (c) the difference. (d–f) as in (a–c) except for time-mean eddy geostrophic wind work \( (P_{ge}) \). Dots representing the statistical significance at 95% confidence level. (g) Zonally integrated \( P_{gm} \) and \( P_{ge} \) (m\(^3\text{s}^{-3}\)) as a function of latitude.

3.3. Energetics of geostrophic eddy activity

What is the consequence of the reduced geostrophic wind work on the energetics of the general and mesoscale circulation? Fig. 5 compares the climatologies of EKE and mean kinetic energy (MKE). For EKE, the altimeter-based estimate is also provided for comparison. The comparison suggests that the model underestimates the high EKEs observed to the south of the separated EICC latitude and along the northwestern coast. This difference stems in part from the bias in the simulated surface circulation in the model as the model underestimates the southwestward branch of the EICC northern BoB (Fig. 3e and f) and thus the associated eddy fields there. Nevertheless, the simulated EKE is in gross agreement with the altimeter-based estimate in terms of magnitude; in both cases, the EKEs exceed 0.1 m$^2$s$^{-2}$ along the EICC path and its separated latitude. As with the strength of the geostrophic current and wind work, the EKE in noRW is too strong compared to that in CTL; the area-averaged percent difference in EKE climatologies can be nearly 100%. This is also the case with the MKE. The change in MKE would be translated into the EKE through the altered barotropic conversion process in the EKE budget equation (next section).

On the one hand, the damping of EKE due to the RW effect is consistent with the finding from a recent study on the Somali Current (Seo, 2017) and other boundary currents and their extensions (Zhai and Greatbatch, 2007; Eden and Dietze, 2009; Seo et al., 2016; Renault et al., 2016a,b). In these boundary current systems, however, the reduction of EKE due to the RW effect is in range of 20–50%, much smaller than what we find in the BoB. We note that the magnitude of the change in wind work due to RW is comparable to the previous studies. This leads to an intriguing question as to why the EKE damping by the RW effect is particularly strong in the BoB given the similar change in wind work. We are not clear about this at this point, although we suspect that it might have to do with the strong salinity stratification in the BoB compared to other basins. This investigation is ongoing and will be reported elsewhere.

To quantify the causes of the changes in the EKE, the three diagnostic quantities that represent energy sources and energy conversions are derived from the equations of motion:

$$P = P_n + P_i = 1 \rho_0 \left( \langle u'v' \rangle + \langle v'w' \rangle \right) + 1 \rho_0 \left( \langle u'' \rangle + \langle v'' \rangle \right)$$

(4)

$$BC_{FE \rightarrow KE} = - \frac{g}{\rho_0} \int_{-h}^{0} \left( \langle \rho' \omega' \rangle + \langle \rho'' \omega'' \rangle \right) dz$$

(5)

Eq. (4) represents the total work done by the wind stress on the ocean, which can be separated into the mean component ($P_n$) affecting the MKE and then EKE through barotropic energy conversion, and the eddy wind work ($P_i$), which enters the EKE budget equation as a source or sink. Eq. (5) denotes the eddy conversion from potential to kinetic energy, particularly important during baroclinic instability (BC). Eq. (6) represents the conversion from MKE to EKE, which is dominated by the horizontal and vertical Reynolds stresses indicative of barotropic instability (BT) and vertical shear instability. We will treat these horizontal and vertical Reynolds stresses as collectively the barotropic process (BT). Given that the kinetic energy decreases significantly below 300 m (Chen et al., 2018), the terms in (4–6) are integrated within prevailing the top 300 m, i.e. $h = 300$ m.

The results are presented as the climatological differences in each of these terms. The changes in depth-integrated MKE and EKE are similar to those at the surface (Fig. 5), thus not shown. Fig. 6 shows $P_n$, $P_i$, BT, and BC, in addition to their zonally integrated meridional profiles, color-coded to denote CTL (orange) and noRW (blue). As was discussed before, both the wind work, $P_n$ and $P_i$, are reduced in CTL (see Table 1), the most pronounced in the western basin. This is also the region of the most energetic eddy activity. The reduced MKE in CTL is translated into the reduced EKE by affecting the shear of the mean and eddy currents, and thus the BT, especially between the EICC and the strong eddying region to the south. On the other hand, BC is increased by 11%; the increase in depth-integrated baroclinic energy conversion is unable to explain the reduced EKE in CTL. When zonally integrated, the contribution of changes in BT and BC to the EKE tendency is an order of magnitude smaller than the changes in the eddy wind work, suggesting that the difference in EKE between two runs is a direct result from the difference in the eddy wind work.

We also examine the scale-dependence of the changes in energy and its source terms. The top panel of Fig. 7 shows the zonal wavenumber spectra of the surface EKE and EKE tendency and in the bottom the co-spectra between the eddy current and eddy stress and the mean current and mean stress. The spectra were calculated across the zonal width of
the Bay (82°-96°E) over the latitudes of 12°–16°N, where the EKE change was the largest, and then the individual spectra were averaged in this latitude band. Also indicated in the right axis of each panel is the percent difference in the spectra, with the negative quantities denoting that the variance is reduced in CTL. We present the co-spectra of current and wind stress instead of the spectra of wind work since the interpretation of the spectrum of a product of two variables can be ambiguous in that the convolution of the spectra of two different variables mixes the signal in spectral space. Nevertheless, we did calculate the spectra of the eddy and mean work to find that the results are in general very similar to those from the co-spectra (not shown).

The previous section discussed how the change in geostrophic wind work has led to changes in geostrophic eddy activity. The current section explores the impacts on the upper ocean stratification and MLD.
The top panel of Fig. 8 compares the JJAS climatologies of the MLD and the 20°C isothermal layer depth (D20), a proxy for the thermocline depth, along with their differences. MLD is estimated as the depth at which the increase in density from the surface becomes equivalent to the temperature decrease by 0.3°C (the result is relatively insensitive to the choice of criteria). The simulated summer MLD is broadly consistent with the previous estimates based on in situ and Argo data (e.g., Narvekar and Prasanna Kumar, 2014; Prend et al., 2018), showing the deep MLD in the central Bay at 12°-14°N of 30-35 m with the secondary maximum along the western Bay and the gradual northward shoaling following the increasing stratification to the north. However, there are also apparent biases in the simulated MLD compared to other observations-based estimates (e.g., De Boyer Montégut et al., 2007), which may be due to the subjective treatment of river runoff in the model, not...
to mention the bias in the wind speed (not shown). Between CTL and noRW, the CTL MLD becomes overall shallower in the western and northern basin but deeper in the central basin. However, the changes are mostly insignificant at 95% level except for the region south of the EICC, the area enclosed by the contour of MLD shoaling in CTL by 2 m (black contour in Fig. 8c). There, MLD shoals by up to 5 m where the climatological MLD is 20 m. A similar result can be found from the changes in D20, albeit smaller and less significant, which shows the shoaling by up to 10 m where the climatological D20 is about 120 m.

What causes the MLD to shoal with the RW effect? Fig. 9a and b compares the difference of the Brunt-Väisälä frequency (N^2) and the vertical shear of horizontal current (S^2), both averaged over the thermocline depth (D20), (c) energy required for mixing (ERM) the D20, and (d) available turbulent kinetic energy (ATKE) from surface to the D20. (e) Percent changes in the JJAS climatology of Ekman vertical velocity due to current-wind interaction (W_e) and (f) that due horizontal vorticity gradient (W_ς). Dots represent the significance of the difference at 95% level. The black contour in (c) and (f) denote the area of MLD reduction by 2 m.

Fig. 9. Percent changes in the JJAS climatology of (a) Brunt-Väisälä frequency (N^2) and (b) vertical shear of horizontal current (S^2), both averaged over the thermocline depth (D20), (c) energy required for mixing (ERM) the D20, and (d) available turbulent kinetic energy (ATKE) from surface to the D20. (e) Percent changes in the JJAS climatology of Ekman vertical velocity due to current-wind interaction (W_e) and (f) that due horizontal vorticity gradient (W_ς). Dots represent the significance of the difference at 95% level. The black contour in (c) and (f) denote the area of MLD reduction by 2 m.

where \( \nu^* \) denotes the friction velocity, \( \rho \) the sea water density, \( \epsilon_m \) the background dissipation, taken as \( 2 \times 10^{-8} \) m$^2$s$^{-3}$ (Shetye, 1986), and \( h \) the D20. The first term on the right-hand side represents the generation of the TKE, and the second term the dissipation. Here, \( \eta_G \) is treated as constant 1.25 (Kraus and Turner, 1967; Alexander and Kim, 1976; Shetye, 1986; Parekh et al., 2011). Indeed, the area of increased wind stress and less reduced S^2 marks the enhanced ATKE there. Based on this consideration, the increase in the near-surface turbulence is unable
to explain the reduced MLD there.

On the other hand, $N^2$ increases precisely where MLD is shoaled, so the increase in the upper ocean stratification can be considered as the chief reason for the reduced MLD. To show this, we calculated the energy required for mixing (ERM), following Shenoi et al. (2002) and Agarwal et al. (2012) as

$$
ERM = \frac{1}{g} (\rho_b - \rho_s) gh^2,
$$

where $\rho_b$ and $\rho_s$ are the bulk and surface layer density, respectively and $h$ as taken at D20. Physically, ERM represents the difference in potential energy (PE) per unit area before and after mixing (Cushman-Roisin and Beckers, 2011). The PE before mixing is estimated given the simulated stratification in CTL and noRW, while PE after the mixing is estimated assuming the upper ocean has been vertically well mixed. Since ERM represents the upper ocean stratification, the pattern and magnitude of the change in ERM (Fig. 9c) are expected to reflect those of $N^2$ and the MLD, with the most substantial increase in the region of the maximum MLD shoaling.

The increased $N^2$ and the shoaled ML with the RW can also be illustrated in Fig. 10 showing the depth-longitude diagrams of the density, $N^2$, and $S^2$ over 12–15°N where the anticyclonic eddy fields are dominant. The colored contours denote the lines of constant density, $N^2$, and $S^2$ for CTL and noRW, while the differences (CTL-noRW) are shown as the shading. The average MLD and D20 are repeated in each of the figures. Dots denote the areas of significant difference at 95% confidence level, evaluated a Monte Carlo bootstrap sampling. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

The percent change in $W_{\zeta}$ shows a dipole structure straddling the region of maximum MLD reduction, with a slight upward velocity in the northwest and downward in the southeast. However, the overall change pattern is less coherent, the actual magnitude of increase in $W_{\zeta}$ is $\sim$10–20 cm day$^{-1}$, i.e. for 120 days per each summer, this anomalous upward motion can alone raise the isopycnals by $\sim$12–24 m. Considering other processes at work, this is broadly consistent with the D20 change shown in Fig. 8f.

The percent change in $W_{\beta}$ is found to be at least an order of magnitude smaller than the first two terms, and thus it is not considered in the subsequent analysis. The percent differences between the first two terms are shown in Fig. 9e and f. In CTL, there is anomalous upward $W_c$, which is stronger by 100% than that in noRW. The actual amount of increase in the upward $W_c$ is $\sim$10–20 cm day$^{-1}$, i.e. for 120 days per each summer, this anomalous upward motion can alone raise the isopycnals by $\sim$12–24 m. Considering other processes at work, this is broadly consistent with the D20 change shown in Fig. 9f.

$$
W_{\text{tot}} = W_f + W_{\zeta} + W_{\beta},
$$

Here, the final term, $W_{\beta}$, is found to be at least an order of magnitude smaller than the first two terms, and thus it is not considered in the subsequent analysis. The percent differences between the first two terms are shown in Fig. 9e and f. In CTL, there is anomalous upward $W_c$, which is stronger by 100% than that in noRW. The actual amount of increase in the upward $W_c$ is $\sim$10–20 cm day$^{-1}$, i.e. for 120 days per each summer, this anomalous upward motion can alone raise the isopycnals by $\sim$12–24 m. Considering other processes at work, this is broadly consistent with the D20 change shown in Fig. 8f.

The percent change in $W_c$ shows a dipole structure straddling the region of maximum MLD reduction, with a slight upward velocity in the northwest and downward in the southeast. However, the overall change pattern is less coherent, the actual magnitude of increase in $W_c$ is by order of magnitude smaller than that of $W_s$, and the change fails to be significant. Therefore, the shoaling of MLD is associated with the doming isopycnals due to anomalous upward Ekman vertical motion...
brought about by the RW effect. The rise of the thermocline enhances
the near-surface stratification (Fig. 10b). In this region, the wind stress
and current are in the opposite direction so the increased ATKE can
ensue, slightly countering this increased stratification.

3.5. Idealized eddy-wind interaction

The shoaling of the MLD through the Ekman upwelling velocity is
further illustrated in Fig. 11, which depicts realistic and idealized sce-
narios of sea level anomaly under the southwesterly monsoonal winds.
Fig. 11a shows the climatologies of sea level anomaly and 10-wind
vectors in the southwestern BoB from CTL. The mean conditions ef-
ctively illustrate the anticyclonic eddy with a radius \( r_0 \) of \( \sim 200 \) km and an amplitude \( A \) of \( 25 \) cm, as measured based on the difference in
sea level between the eddy center \( \eta_c \) and the ambient water \( \eta_a \). This
eddy interacts with the nearly uniform southwesterly surface wind with
a speed of \( 7 \) ms\(^{-1}\).

This anticyclonic eddy is approximated in an idealized considera-
tion as an axis-symmetric Gaussian eddy, whose sea level anomaly \( \eta \)
vary as a function of the radial distance,

\[
\eta(r) = \eta_a + A \exp \left( -\frac{r^2}{r_0^2} \right) \tag{10}
\]

where we take \( \eta_a = 50 \) cm, \( A = 25 \) cm, and \( r_0 = 200 \) km based on
Fig. 11a. This eddy is shown as shading in Fig. 11b. The induced
geostrophic surface currents (green vectors) have a maximum speed of
0.27 ms\(^{-1}\) at the eddy boundary and turn anticyclonically. The super-
posed black vectors denote the uniform surface wind of \( 7 \) ms\(^{-1}\), re-
miniscent of the realistic situation depicted in Fig. 11a. Here, for sim-
plicity, we assume there is no SST signature associated with this
anticyclonic eddy, although previous studies amply suggest that SST-
duced perturbation in wind and wind stress can be substantial (Gaube
et al., 2015; Seo et al., 2016; Seo, 2017; Laurindo et al., 2018).

In this scenario, because the surface current is opposite to the wind
stress, the RW effect creates the anomalous wind stress that turns cy-
clonically (black vectors in Fig. 11c). The shading in Fig. 11c denotes
\( W_{tot} \) calculated from Eq (9), which reveals the upward velocity of up to
0.30 cm day\(^{-1}\) northwest of the eddy center and the comparatively
weaker downward velocity in the southeast. This \( W_{tot} \) results from the
combined effect of the two components, \( W_c \) and \( W_\varsigma \), as shown sepa-
ately in Fig. 11d and e. The amplitude and pattern of the perturbation

![Fig. 11. (a) The simulated summertime climatologies in CTL: SSH (color shading), surface geostrophic current (green vectors), and surface wind (black vectors). (b) An idealized axis-symmetric Gaussian anticyclonic eddy interacting with the spatially uniform monsoon winds of 7 ms\(^{-1}\) (black vectors) through the surface geostrophic current (green vectors). The gray contours denote the SSHA at 5 cm interval, which is repeated in (c–e) to represent the position of the anticyclonic eddy. (c) The induced wind stress fields (black vectors) overlaid with the total Ekman vertical velocity \( W_{tot} \) (cm day\(^{-1}\), positive upward). (d–e) The separation of the \( W_{tot} \) into (d) that due to the relative wind effect (\( W_c \)) and (e) that due to vorticity gradient (\( W_\varsigma \)). This figure was inspired by Chelton (2013). (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)](image-url)
$W_e$ suggest the RW effect alone would create the maximum upward velocity up to 20 cm day$^{-1}$ (or $\sim$24 m per summer) right over the eddy center, consistent with the result from Fig. 9e. The RW effect thus exerts the significant and direct damping effect on the amplitude of the anticyclonic eddy. On the other hand, $W_c$ features a dipole pattern with the upward velocity in excess of 10 cm day$^{-1}$ in the northwest of the eddy center and downward of the similar magnitude in the southeast, qualitatively consistent with what was shown in Fig. 9f. When $W_e$ and $W_c$ are combined together, one can expect that, while the spatial pattern of $W_{tot}$ is influenced by $W_c$, overall the RW effect is dominant and significantly damps the anticyclonic eddy by doming the isopycnals.

According to McGillicuddy (2015), the RW effect through the eddy-wind interaction can alone transform an anticyclonic eddy into a mode-water eddy through anomalous Ekman vertical velocity. Our study implies that the vertical structure of the isopycnals of the anticyclonic eddy responds similarly, although this is only true in a relative sense. That is, the anticyclonic eddy itself in Fig. 11a is not of a mode-water type, but the process affecting the eddy vertical structure through the RW effect is consistent with the formation mechanism of a mode-water eddy by McGillicuddy (2015). A mode-water eddy was observed in the western Bay of Bengal in winter of 2013 by Gordon et al. (2017), whose formation was also attributed to a result of the interaction of a tropical cyclone with an anticyclonic eddy through air-sea fluxes. Our study suggests that the eddy-wind interaction through the surface current, whether or not the wind is kept spatially uniform as in our idealized case, rotates as considered in an idealized model of McGillicuddy (2015), or is entirely transient as in a fully coupled model, could altogether generate the anomalous upward velocity, doming the isopycnals and enhancing the stratification below the ML. This effect outweighs the enhanced near-surface turbulence, and when combined, the RW effect shoals the MLD over the anticyclonic eddy.

4. Summary and discussion

This study examines the effect of the inclusion of surface currents, so-called the relative wind (RW) effect, in the bulk formula on the wind work, the Ekman vertical velocities, and the energetics and dynamics of the circulation in the Bay of Bengal (BoB) in summer. Our high-resolution (5 km) SOOAR regional coupled model simulation with explicit convection in the atmosphere captures the RW effect due to the well-resolved surface currents in the ocean (CTL), while an indication of its importance in the overall climatology of the BoB circulation and mixed layer depth (MLD) was identified with an identical twin-experiment where the RW effect is excluded in the bulk formula (noRW).

The results show that the energetics of the mean and eddy geostrophic circulation is significantly reduced with the RW effect, improving the realism of the model simulations. This damping effect is most significant south of the separated latitude of the East India Coastal Current (EICC) at 16°N, where the kinetic energy, both the eddy (EKE) and mean (MKE), is reduced in CTL by more than a factor of two. Comparison of the energy source and the depth-integrated barotropic and baroclinic energy conversion processes reveals that the mean geostrophic wind work represents the most significant source of energy for the BoB, which is reduced by 39% in CTL with the RW effect. The eddy wind work is smaller by a factor of 5 than the geostrophic wind work, but the sign of this term switches from positive (energy source) to negative (energy sink) in CTL. The eddy wind work enters the EKE budget equation as a source or sink depending on its sign, so this sign change is critical for the EKE reduction in CTL. The mean wind work, on the other hand, translated into the changes in barotropic energy conversion, which, despite achieving as large amplitude as the eddy wind work locally, is still an order of magnitude smaller than the mean wind work when integrated over the Bay. Likewise, the depth-integrated baroclinic conversion processes account for only a small fraction of the EKE tendency and in fact increases in CTL. It is unable to explain the reduced EKE.

Further insights into the changes in the eddy energetics can be gained by comparing the zonal wavenumber spectra of each of these terms. The dramatic decline of the EKE and EKE tendency takes place over wavelengths of around 100 km, the scale of the geostrophic eddy fields that corresponds to the first baroclinic Rossby deformation radius in the southern BoB. These wavelength bands coincide with the wavelengths of the significant reduction of the eddy wind work. Furthermore, there is little difference between the spectra of wind work and the co-spectra of the wind and current. These suggest that the RW effect on wind work and EKE arises from the linear, scale-to-scale coupling between the wind and current.

We also examined the changes in MLD, upper ocean stratification, and Ekman vertical velocities. MLD and, to a lesser extent, thermocline depth (DD0), are both shoaled with the RW effect, again most significantly in the southwestern basin of strong anticyclonic eddy activity. Further analysis reveals that, while vertical shear of horizontal currents ($S^2$) is broadly reduced, the available turbulent kinetic energy (ATKE) is actually increased where the MLD is shoaled. This ATKE increase is because the wind and surface currents are in the opposite direction, which enhances the stress and wind work. Therefore, the increased near-surface turbulence cannot account for the decreased MLD. On the other hand, both the Brunt-Väisälä frequency ($N^2$) and the energy required for mixing (ERM) are significantly increased in this region of reduced MLD. The vertical sections across the region of strong anticyclonic eddy activity show the increase in density and stratification below the MLD and above the thermocline in CTL.

The question then became what causes the stratification to increase with the RW effect? We suggest that the upward Ekman upward velocity due to RW effect and the induced doming of the isopycnals is mainly responsible. The mechanism is reminiscent of what McGillicuddy (2015) suggested to explain the transformation of an anticyclonic eddy with the positive sea level anomaly into a mode-water type eddy through local eddy-wind interaction. The current-induced Ekman vertical velocity over the anticyclonic eddy is directed upward, doming the isopycnals, and in the process, enhancing the near-surface stratification. On the other hand, the change in Ekman vertical velocity induced by the horizontal vorticity gradient is insignificant, spatially incoherent, and out of phase with the changes in stratification and MLD, and thus its significance to the anomalous doming of the isopycnals in CTL to shoal the MLD could be ruled out.

Finally, this study demonstrated a rather substantial reduction of the energetics of the ocean currents near the EICC due to the RW effect, compared to other ocean boundary currents. In other boundary current systems, the EKE modulation by the RW effect was found in the range of 20–50%, compared to 100% as seen in this study. What makes the BoB so sensitive to the RW effect remains unclear, although one could speculate that the strong upper ocean stratification in the BoB, the distinguishing feature from the rest of the ocean basins, could offer a possible answer. One might also suspect the effects of surface gravity waves affecting the wind stress through wave-current interactions (Bye, 1986; Johannessen et al., 1996). Though this process was not considered explicitly in this study, we note that the bulk formula uses the sea-state dependent formulation of the drag coefficient (Fairall et al., 1996, 2003; Edson et al., 2013), which is adopted in the study. The strong monsoon winds over the BoB in the boreal summer support intensified surface wave fields (Shanas and Kumar, 2014; Anoop et al., 2015), whose effect on the air-sea momentum flux could be important for more realistic simulations of the BoB circulation (Jensen et al., 2016). This is a subject of ongoing investigations using idealized ocean-model simulations with different background density stratification and waves effects.

Regardless of the mechanisms responsible for the considerable sensitivity of the eddy energetics to the RW effect in the BoB, the results from our experiments imply that to advance our understanding of the upper ocean circulation and the energy pathways, as well as their subsequent coupling with the wind and atmosphere, requires well-
resolved, simultaneous measurements of the surface current and wind in the BoB, as well as detailed upper ocean stratification and vertical mixing. This has been the focus of recent several international research activities anchored in the BoB (Wijesekera et al., 2016; Mahadevan et al., 2016; Vinayachandran et al., 2018). From these research programs combining the extensive measurements of the upper ocean and meteorological variability with the process-oriented numerical model simulations of various kinds, we expect to advance our understanding of the role of the ocean and air-sea interactions in the monsoon circulation dynamics in the ocean and atmosphere and to improve their representation in simulation and prediction models.

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References
